

ECE408 / CS483 / CSE408 Summer 2024

Applied Parallel Programming

Lecture 4: Memory Model

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What Will You Learn Today?

- basic features of the memories accessible by CUDA threads
- concepts for Lab 2: basic matrix multiplication
- to evaluate the performance implications of global memory accesses

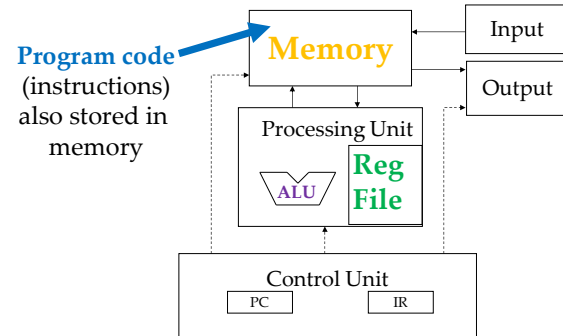
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Von-Neumann Model Abstracts Computer as Five Parts



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Instructions are Stored in Memory

- Every instruction needs to be fetched from memory, decoded, then executed.
- Instruction processing breaks into steps:
Fetch | **Decode** | **Execute** | **Memory**
- Instructions come in three flavors:
Operate, Data Transfer, and Control Flow.

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Example: Processing an Add Instruction

- Example of an (LC-3) operate instruction:

ADD R1, R2, R3

- meaning:
 - read R2 and R3
 - **add them as unsigned/2's complement**
 - write sum to R1

- Instruction processing for an operate instruction:

Fetch | Decode | Execute | Memory

Example: Processing a Load Instruction

- Example of an (LC-3) data transfer instruction:

LDR R4, R6, #3 ; a load

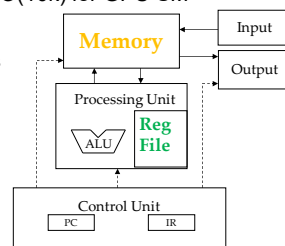
- meaning:
 - read R6
 - **add the number 3 to it**
 - **load the contents of memory at the resulting address**
 - write the bits to R4

- Instruction processing for a load instruction:

Fetch | Decode | Execute | Memory

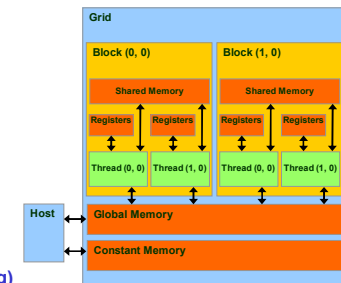
Registers vs Memory

- **Registers**
 - Fast: 1 cycle; no memory access required
 - Few: hundreds for CPU, O(10k) for GPU SM
- **Memory**
 - Slow: hundreds of cycles
 - Huge: GB or more



Programmer View of CUDA Memories

- Each thread can:
 - read/write per-thread **registers (~1 cycle)**
 - read/write per-block **shared memory (~5 cycles)**
 - read/write per-grid **global memory (~500 cycles)**
 - read/only per-grid **constant memory (~5 cycles with caching)**



CUDA Variable Type Qualifiers

Variable declaration	Memory	Scope	Lifetime
<code>int LocalVar;</code>	register	thread	thread
<code>__device__ __shared__ int SharedVar;</code>	shared	block	block
<code>__device__ int GlobalVar;</code>	global	app.	application
<code>__device__ __constant__ int ConstantVar;</code>	constant	app.	application

- `__device__`
 - optional with `__shared__` or `__constant__`
 - not allowed by itself within functions
- Automatic variables with no qualifiers
 - in registers for primitive types and structures
 - in global memory for per-thread arrays

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Next Application: Matrix Multiplication

- Given two $Width \times Width$ matrices, M and N,
 - we can multiply M by N
 - to compute a third $Width \times Width$ matrix, P:
 - $P = MN$.

In terms of the elements of P, matrix multiplication implies computing...

$$P_{ij} = \sum_{k=1}^{Width} M_{ik} N_{kj}$$

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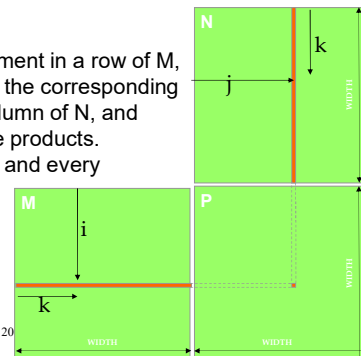
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Matrix Multiplication

$$P_{ij} = \sum_{k=1}^{Width} M_{ik} N_{kj}$$

- Graphically, imagine
 - taking each element in a row of M,
 - multiplying it by the corresponding element in a column of N, and
 - summing up the products.
- Do that for every row and every column to produce P.



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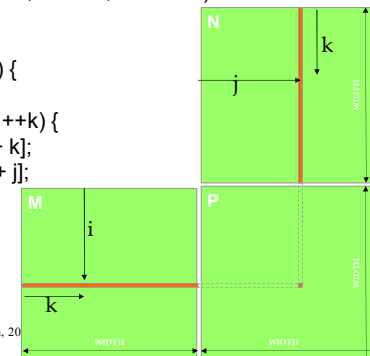
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Sequently Matrix Multiplication in C

// Matrix multiplication on the (CPU) host in single precision
void CPUMatMul(float* M, float* N, float* P, int Width)

```
{
  for (int i = 0; i < Width; ++i)
    for (int j = 0; j < Width; ++j) {
      float sum = 0;
      for (int k = 0; k < Width; ++k) {
        float a = M[i * Width + k];
        float b = N[k * Width + j];
        sum += a * b;
      }
      P[i * Width + j] = sum;
    }
}
```



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Parallelize Elements of P

- What can we parallelize?
 - start with the **two outer loops**
 - parallelize **computation of elements of P**
- What about the inner loop?
 - Technically, floating-point is NOT associative.
 - The **parallel sum** is called a **reduction**—we'll return to it in a few weeks.
 - For now, **use a single thread for each P_{ij}**.

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Compute Using 2D Blocks in a 2D Grid

- **P** is 2D, so organize threads in 2D as well:
 - Split the output **P** into square **tiles**
 - of size **TILE_WIDTH × TILE_WIDTH**
 - (a preprocessor constant).
 - **Each thread block produces one tile** of TILE_WIDTH^2 elements.
 - Create $\lceil \text{Width} / \text{TILE_WIDTH} \rceil^2$ thread **blocks** to cover the output matrix.

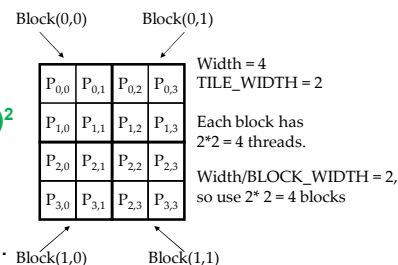
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Kernel Function - A Small Example

- Each 2D thread block
 - has $(\text{TILE_WIDTH})^2$ threads and
 - computes a $(\text{TILE_WIDTH})^2$ sub-matrix of the result matrix.
- Generate a 2D Grid of $(\text{Width}/\text{TILE_WIDTH})^2$ blocks.
- Concept called **tiling**, and each **block computes a tile**.



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Example: Width 8, TILE_WIDTH 2

P _{0,0}	P _{0,1}	P _{0,2}	P _{0,3}	P _{0,4}	P _{0,5}	P _{0,6}	P _{0,7}
P _{1,0}	P _{1,1}	P _{1,2}	P _{1,3}	P _{1,4}	P _{1,5}	P _{1,6}	P _{1,7}
P _{2,0}	P _{2,1}	P _{2,2}	P _{2,3}	P _{2,4}	P _{2,5}	P _{2,6}	P _{2,7}
P _{3,0}	P _{3,1}	P _{3,2}	P _{3,3}	P _{3,4}	P _{3,5}	P _{3,6}	P _{3,7}
P _{4,0}	P _{4,1}	P _{4,2}	P _{4,3}	P _{4,4}	P _{4,5}	P _{4,6}	P _{4,7}
P _{5,0}	P _{5,1}	P _{5,2}	P _{5,3}	P _{5,4}	P _{5,5}	P _{5,6}	P _{5,7}
P _{6,0}	P _{6,1}	P _{6,2}	P _{6,3}	P _{6,4}	P _{6,5}	P _{6,6}	P _{6,7}
P _{7,0}	P _{7,1}	P _{7,2}	P _{7,3}	P _{7,4}	P _{7,5}	P _{7,6}	P _{7,7}

Each block has $2 \times 2 = 4$ threads.

WIDTH/TILE_WIDTH = 4
Use $4 \times 4 = 16$ blocks.

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Example: Same Matrix, Larger Tiles (Width 8, TILE_WIDTH 4)

P _{0,0}	P _{0,1}	P _{0,2}	P _{0,3}	P _{0,4}	P _{0,5}	P _{0,6}	P _{0,7}
P _{1,0}	P _{1,1}	P _{1,2}	P _{1,3}	P _{1,4}	P _{1,5}	P _{1,6}	P _{1,7}
P _{2,0}	P _{2,1}	P _{2,2}	P _{2,3}	P _{2,4}	P _{2,5}	P _{2,6}	P _{2,7}
P _{3,0}	P _{3,1}	P _{3,2}	P _{3,3}	P _{3,4}	P _{3,5}	P _{3,6}	P _{3,7}
P _{4,0}	P _{4,1}	P _{4,2}	P _{4,3}	P _{4,4}	P _{4,5}	P _{4,6}	P _{4,7}
P _{5,0}	P _{5,1}	P _{5,2}	P _{5,3}	P _{5,4}	P _{5,5}	P _{5,6}	P _{5,7}
P _{6,0}	P _{6,1}	P _{6,2}	P _{6,3}	P _{6,4}	P _{6,5}	P _{6,6}	P _{6,7}
P _{7,0}	P _{7,1}	P _{7,2}	P _{7,3}	P _{7,4}	P _{7,5}	P _{7,6}	P _{7,7}

Each block has
4*4=16 threads.

WIDTH/TILE_WIDTH = 2
Use 2*2 = 4 blocks.

Kernel Invocation (Host-side Code)

```
// TILE_WIDTH is a #define constant
dim3 dimGrid(ceil((1.0*Width)/TILE_WIDTH),
             ceil((1.0*Width)/TILE_WIDTH), 1);
dim3 dimBlock(TILE_WIDTH, TILE_WIDTH, 1);

// Launch the device computation threads!
MatrixMulKernel<<<dimGrid, dimBlock>>>
    (Md, Nd, Pd, Width);
```

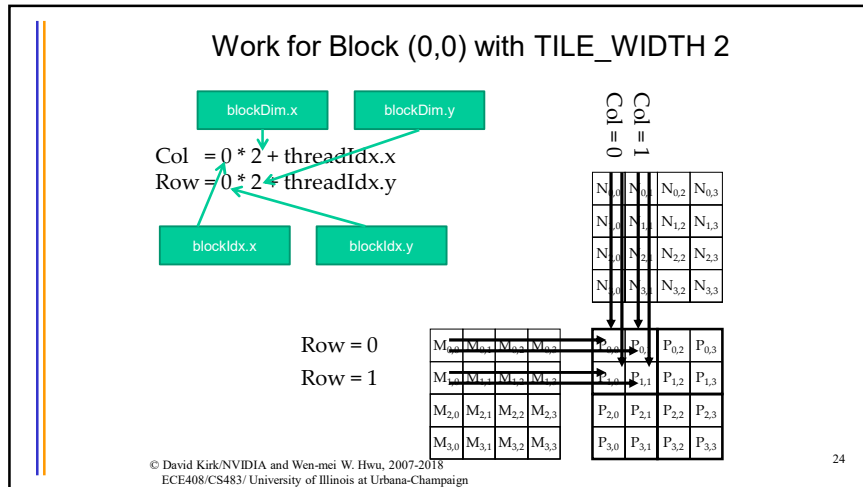
Kernel Function

```
// Matrix multiplication kernel - per thread code
__global__
void MatrixMulKernel(float* d_M, float* d_N, float* d_P, int Width)
{
    // Pvalue is used to store the element of the matrix
    // that is computed by the thread
    float Pvalue = 0;
    ...
    ...
    d_P[ ] = Pvalue;
```

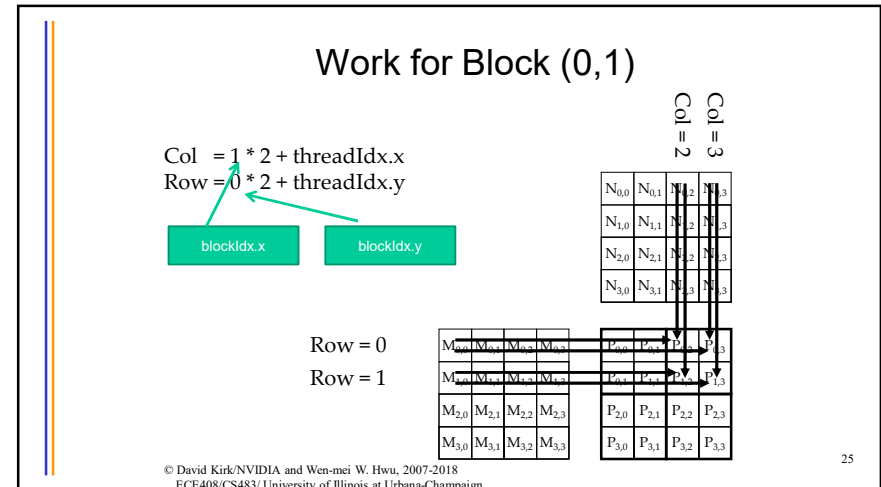
Compute Row & Col for Each Thread

```
// Calculate the row index of the d_P element and d_M
int Row = blockIdx.y * blockDim.y + threadIdx.y;

// Calculate the column index of d_P and d_N
int Col = blockIdx.x * blockDim.x + threadIdx.x;
```



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A Simple Matrix Multiplication Kernel

```

__global__ void MatrixMulKernel(float* d_M, float* d_N, float* d_P, int Width)
{
    // Calculate the row index of the d_P element and d_M
    int Row = blockIdx.y*blockDim.y+threadIdx.y;
    // Calculate the column index of d_P and d_N
    int Col = blockIdx.x*blockDim.x+threadIdx.x;

    if ((Row < Width) && (Col < Width)) {
        float Pvalue = 0;
        // each thread computes one element of the block sub-matrix
        for (int k = 0; k < Width; ++k)
            Pvalue += d_M[Row*Width+k] *
                    d_N[k*Width+Col];
        d_P[Row*Width+Col] = Pvalue;
    }
}
  
```

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- ### Memory Bandwidth is Overloaded!
- That's a **simple implementation**:
 - GPU kernel is the **CPU code**
 - with the **outer loops replaced**
 - with per-thread **index calculations!**
 - Unfortunately, performance is quite bad.
 - Why?
 - With the given approach,
 - global **memory bandwidth**
 - can't** supply enough data
 - to **keep the SMs busy!**
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Where Do We Access Global Memory?

```

__global__ void MatrixMulKernel(float* d_M, float* d_N, float* d_P, int Width)
{
    // Calculate the row index of the d_P element and d_M
    int Row = blockIdx.y*blockDim.y+threadIdx.y;
    // Calculate the column index of d_P and d_N
    int Col = blockIdx.x*blockDim.x+threadIdx.x;

    if ((Row < Width) && (Col < Width)) {
        float Pvalue = 0;
        // each thread computes one element of the block sub-matrix
        for (int k = 0; k < Width; ++k)
            Pvalue += d_M[Row*Width+k] *
                    d_N[k*Width+Col];
        d_P[Row*Width+Col] = Pvalue;
    }
}

```

accesses to global memory

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Each Thread Requires 4B of Data per FLOP

- Each threads access global memory
 - for elements of **M** and **N**:
 - 4B each**, or **8B per pair**.
 - (And once TOTAL to **P** per thread—ignore it.)
- With each pair of elements,
 - a thread does a single multiply-add,
 - 2 FLOP**—floating-point operations.
- So for every FLOP,
 - a thread needs 4B** from memory:
 - 4B / FLOP**.

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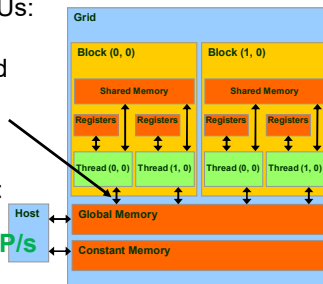
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150 GB/s Bandwidth Implies 37.5 GFLOPs

- One generation of GPUs:
 - 1,000 GFLOPs/s** of compute power, and
 - 150 GB/s** of memory bandwidth.
- Dividing bandwidth by memory requirements:

$$\frac{150 \text{ GB/s}}{4 \text{ B/FLOP}} = 37.5 \text{ GFLOPs/s}$$

which **limits computation!**



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What to Do? Reuse Memory Accesses!

But **37.5 GFLOPs is a limit**.

In an **actual execution**,

- memory is not busy all the time, and
- the code **runs at about 25 GFLOPs**.

To get closer to 1,000 GFLOPs

- we **need to drastically cut down**
- **accesses to global memory**.

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QUESTIONS?

READ CHAPTER 4!

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Problem Solving

- Q: Consider a 2D input matrix of 250 rows and 60 columns. Using 16 x 16 thread blocks of threads to perform operations on the input matrix, with each thread processing one input element, how many blocks need to be launched?
- A:
 - Horizontally, we have 60 columns, so we need $\text{ceil}(60 / 16) = 4$ blocks.
 - Vertically, we have 250 rows, so we need $\text{ceil}(250 / 16) = 16$ blocks.
 - Multiplying the two gives us $4 \times 16 = 64$ thread blocks.

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Problem Solving

- Q: Suppose your kernel code requires certain threads to read data items written by other threads in the same thread block. Which type of memory will be most suitable (fastest accesses) for this purpose?
 - Register
 - Shared memory
 - Global memory
- A: Shared memory

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Problem Solving

- Q: What are the possible values of *dst after this kernel execution?

```
__global__ void kernel(char *dst) {
    dst[0] = blockIdx.x;
}

// dst is a pointer to an array of one char allocated on
// the device and initialized to the value 3 (dst[0]=3 before
// kernel executes).
kernel<<<2,1>>>(dst);
```
- A: Either 0 or 1

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